

Electrical and electronics materials:

- **Response of the material to electric field**
- **Mainly the mobile electrons inside the materials decide the property**
- **The study is done with the help of different simplified models by the scientists**
 - **Classical Free Electron Theory of Metals**
 - **Electrical Conductivity**
 - **Thermal Conductivity**
 - **Quantum Theory of Free Electrons**
 - **Band Theory of Solids**
 - **classification into Conductors, Insulators and semiconductors**

Free Electron Theory

Classical – Drude- Lorenz's Theory (1900) for metals

Assumptions:

- **In materials with metallic bond, the outer electrons are free, i.e., are not bound to any particular metal ion .**
- **These free electrons are non- localized , i.e., instead of confined to a particular atom, they belong to the entire material.**
- **These free electrons move freely and continuously but can not escape the boundary of the metal.**

- **There is no interaction amongst the electrons or between the electrons and positive metal ions. The electrons move in a zero potential field. ($V=0$)**
- **These electrons behave like the particles of a gas and hence called electron gas following all gas laws.**
$$PV = Nk_{\beta} T$$

Av. electron thermal energy= $3/2 k_{\beta} T$
- **The motion of these electrons give rise to conduction of current inside the material.**

Electrical conductivity:

Electron gas:

- Av. Thermal energy of free electrons in the gas is

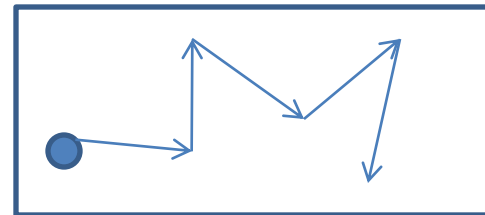
$$E_{av} = \frac{3}{2} k_{\beta} T = \frac{1}{2} m v^2$$

with thermal velocity $v = \sqrt{\frac{3k_{\beta}T}{m_e}} \approx 10^5 \text{ m/s}$

- These free electrons, however are in constant motion & hence collide with each other & with the ions in a solid

- τ is the average time between collision = $\frac{\lambda}{v}$

where λ is the average distance covered between collision is the mean free path



- so, $\tau = \lambda \sqrt{\frac{m_e}{3k_{\beta}T}}$

- $\lambda = 10^5 \times 10^{-14} = 10^{-9} \text{ m} = 1 \text{ nm}$, if $\tau = 10^{-14} \text{ sec}$

When external electric field is applied

- When an ext. electric field is present, the free electrons experience a force and are accelerated with a velocity called “drift velocity”
- $V_d = at$ or $v_d = \frac{F}{m_e} t = qEt/m$
- If $\langle v_d \rangle$ is the average drift velocity and τ is the average collision time, then

$$\frac{d \langle v \rangle}{dt} + \frac{\langle v \rangle}{\tau} = \frac{qE}{m}$$

Solution of the equation gives $\langle v \rangle = \frac{qE\tau}{m} (1 - e^{-\frac{t}{\tau}})$

For small values of τ , the steady state value of drift velocity gives

$$\langle v \rangle = \frac{qE\tau}{m}$$

The current density $J = nq \langle v \rangle = nq \left(\frac{qE\tau}{m} \right) = nq^2\tau E / m$

$J \propto E$ in consistence with Ohm's law

- as according to Ohm's law $\mathbf{J} = \sigma \mathbf{E}$

- Hence electrical conductivity $\sigma = nq^2\tau / m$

$$\text{Also, } \sigma = nq (q\tau / m)$$

But, $q\tau / m = \langle v \rangle / E = \mu$, is the mobility of the electrons, which is drift velocity acquired per electric field.

$$\mu = \langle v \rangle / E = q\tau / m$$

In terms of mobility conductivity can be written as $\sigma = nq \mu$

Electrical resistivity

- Electrical resistivity is the reciprocal of electrical conductivity

$$\text{Hence, } \rho = 1 / \sigma = 1 / nq \mu = m / nq^2 \tau$$

- Resistance is offered due to the collision between the electrons and ions or impurities and defects present inside the material

- $$\rho = m / nq^2 (1 / \tau_{ion} + 1 / \tau_{imp} + 1 / \tau_{def})$$

- $$\rho_{tot} = \rho_{ion} + \rho_{imp} + \rho_{def}$$

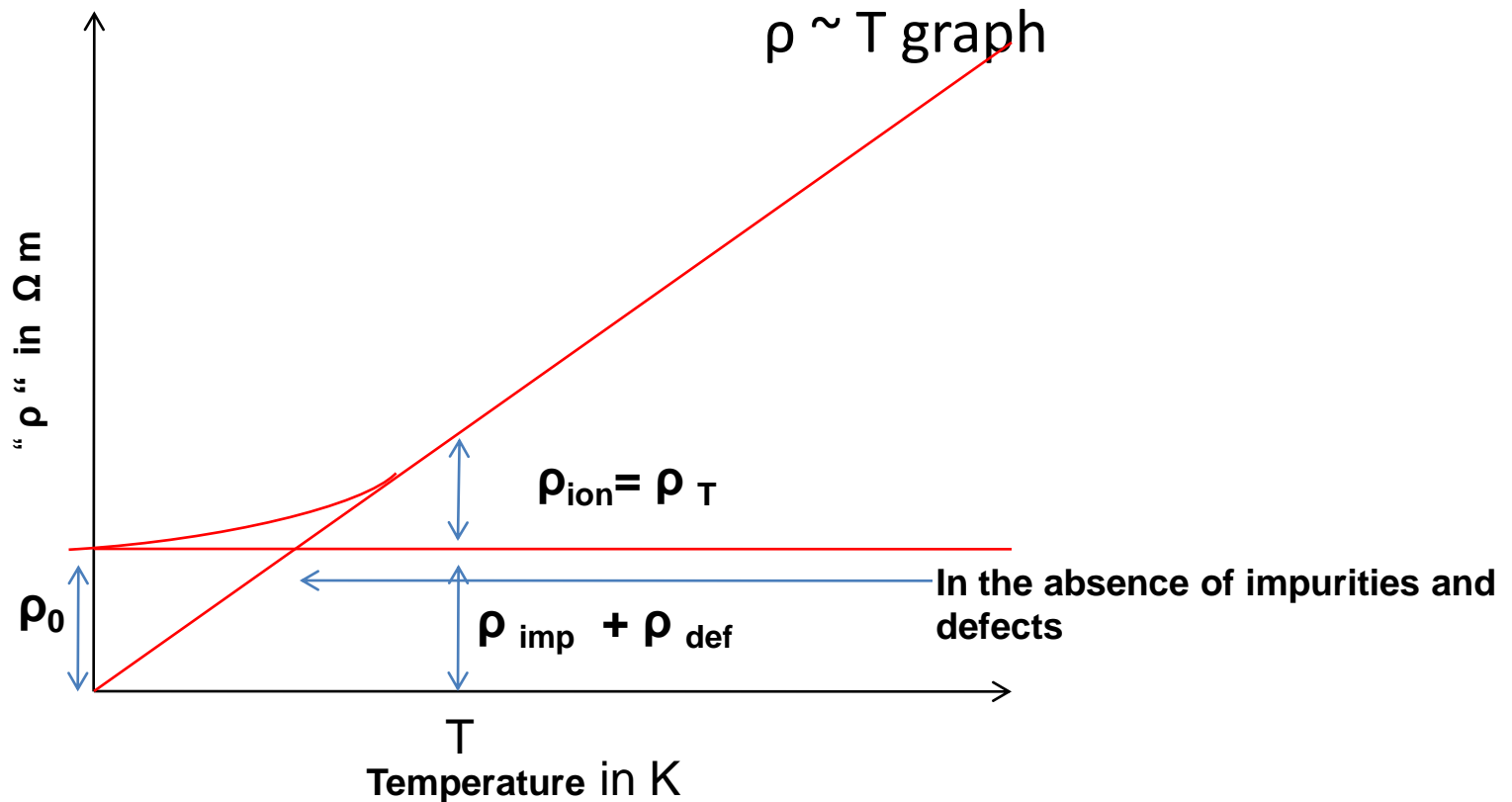
- Out of the three terms in ρ , the first term depends on the temperature, but 2nd and 3rd term do not depend on the temperature. Hence we can write

$$\rho_{\text{tot}} = \rho_0 + \rho(T)$$

This is called Matthiessen's rule

- Mobility depends on the scattering of electrons
- Scattering is caused by phonons(ions) and the impurities and defects
- Scattering by phonons increases with temperature, so resistivity also increases
- Scattering by impurities and defects is independent of temp., but increases with their concentration, hence resistivity also increases $(\rho = m / ne^2\tau = m v / ne^2 \lambda)$
- Resistivity also depends on the magnetic field if present
- Resistivity depend on strain produced as it creates defects

Electrical conductivity and resistivity are the parameters to determine the electrical property



- ρ_0 is called the residual resistivity, which is due to impurities and defects

- **Electrical conductivity and resistivity** are the important parameters to determine the electrical properties of any material
 - i) **high conductivity(low resistivity)**-----metals
 - ii) **low conductivity (even at room temp.)**—ceramics
 - iii) **poor conductivity** ----- polymers
- **Applications:**
 - i) **Zero resistivity materials: Superconductors (Nb,Sn...)**
SC magnets, storage devices, energy saving devices for power system
 - ii) **Low resistivity materials: metals and alloys (Ag,Al...)**
Conductors, electrical contacts, power transmission, wires of motors and transformers
 - iii) **High resistivity: Insulators (W,Pt,Ni....)**
resistors, heating elements, resistance thermometers

THERMAL CONDUCTIVITY

- Heat energy transfer in a material occurs by the vibrating ions (phonons) as well as by the free electron in motion. In a metal the later is dominating. As per Fourier formula for conduction of heat in a solid material is given as

$$Q = KA\left(-\frac{d\theta}{dx}\right)t$$

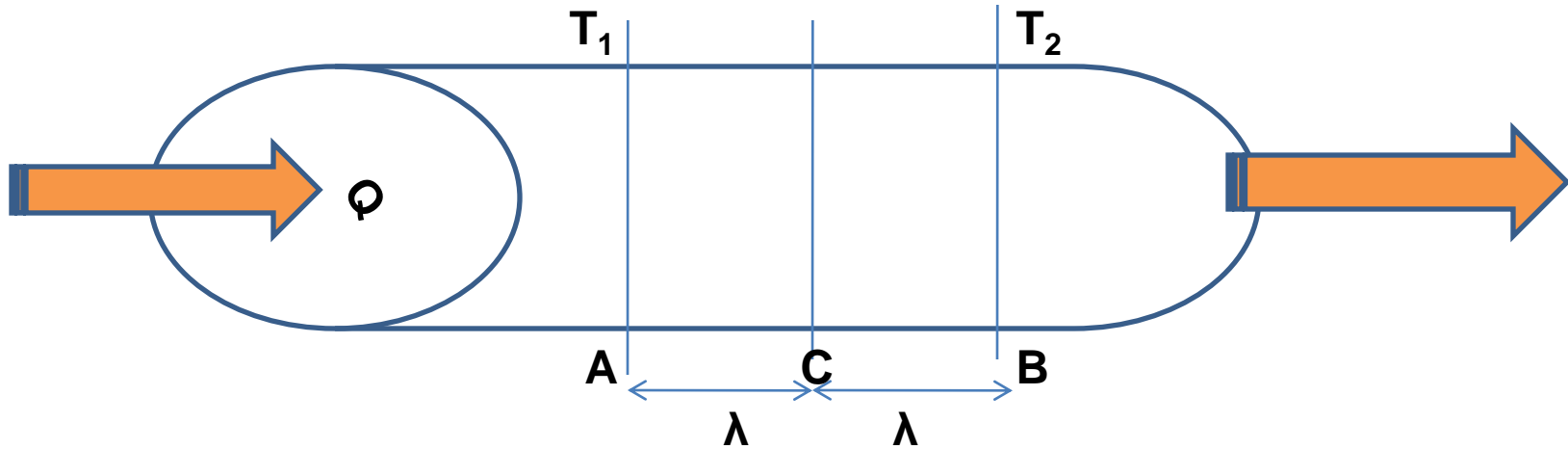
$$\text{Or, } K = J / (-d\theta / dx)$$

Where, $J = Q/At$ = heat flux flowing per area per second

$d\theta / dx$ = temperature gradient

& K = Thermal conductivity of the material i.e., ability to allow heat to pass

- $K = K$ phonon
- In metals K total = K phonon + K electron
- Where K electron \gg K phonon



- Av. Kinetic energy of the electrons at 'A' = $\frac{3}{2} k_{\beta} T_1$
- Av. Kinetic energy of the electrons at 'B' = $\frac{3}{2} k_{\beta} T_2$
- No of electrons crossing 'C' one way per area per second
= $n v_{th} / 6$, n being the electron density

- Net heat energy transferred per second

$$\begin{aligned}
 J &= \left(\frac{nv_{th}}{6}\right) \frac{3}{2} k_{\beta} T_1 - \left(\frac{nv_{th}}{6}\right) \frac{3}{2} k_{\beta} T_2 \\
 &= \frac{nv_{th}}{4} k_{\beta} (T_1 - T_2)
 \end{aligned}$$

Thermal conductivity , $K = J / (- d\theta / dx)$

$$= \frac{nv_{th}}{4} k_{\beta} (T_1 - T_2) \bigg/ \frac{(T_1 - T_2)}{2\lambda}$$

or, $K = \frac{1}{2} n v_{th} k_{\beta} \lambda$

Weideman- Franz law

- In a metal the ratio of thermal conductivity to electrical conductivity is

$$\begin{aligned} K / \sigma &= \frac{\frac{1}{2} n v_{th} k_{\beta} \lambda}{\frac{n q^2 \tau}{m_e}} \\ &= \frac{1 v_{th} k_{\beta} m_e \lambda}{2 q^2 \tau} \\ &= m_e v^2 k_{\beta} / 2 q^2 \\ &= 3 k_{\beta}^2 T / 2 q^2 \quad (\text{as } 3/2 k_{\beta} T = \frac{1}{2} m v^2) \end{aligned}$$

$$K / \sigma = (3 k_{\beta}^2 / 2 q^2) T \quad \text{or, } K / \sigma = L T$$

$$\text{or, } \kappa / \sigma \propto T$$

- This is known as Weideman- Franz law

$L = (3k_B^2 / 2q^2)$ is called the Lorenz No. & is same for all metals = $1.11 \times 10^{-8} \text{ W}\Omega / \text{K}^2$

Merits and demerits of classical free electro theory

Merits: 1. Explains electrical and thermal conductivity

2. Consistence with Ohm's law

3. Explains Weideman- Franz law

4. Explains optical properties

Demerits: 1. Could not explain electronic sp. Heat

2. Could not explain superconducting phenomena

3. $L = \text{constant}$ was not true for all temp. & did not agree with exptl. result

4. Could not explain PE effect, Compton Effect, blackbody radiation & 5. classify materials into semiconductor & insulators